

# 6.1100 Spring 2024 Miniquiz #6

*Please submit your answers on Gradescope by April 11th, 2024, 11:59pm.*

**Name:** [6.110 Staff](#)

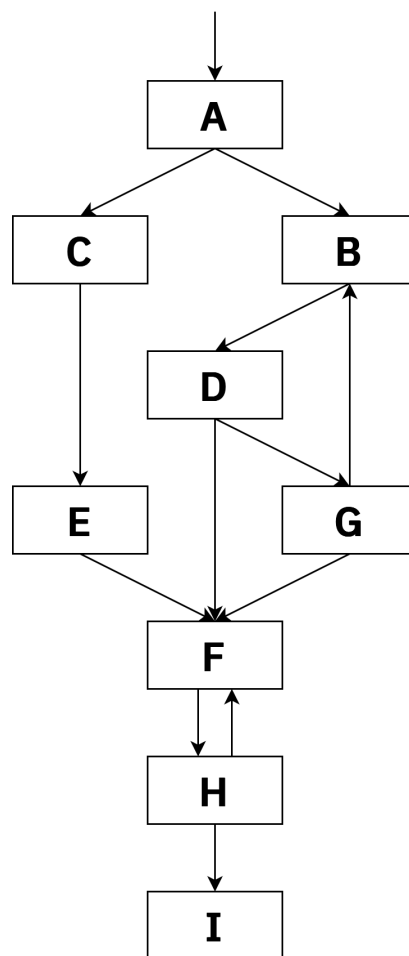
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*Note: This miniquiz covers loop optimizations and parallelization. We will cover register allocation in a later miniquiz.*

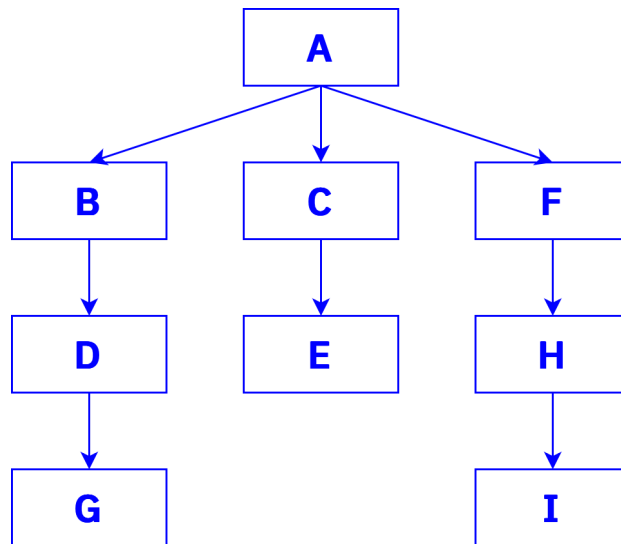
## 1. Loop Optimizations

*(For part a. and b.)*

In the following control flow graph, **A** is the entry node and **I** is the exit node.



- a. Draw the **dominator tree** of this control flow graph.



- b. There are two loops in this control flow graph. Fill in the information about each loop in the table below.

Loop header	Nodes in loop
B	B, D, G
F	F, H

(For part c.-f.)

Consider the following program.

```
1 x = 0;
2 y = 5;
3 while (x < 10) {
4     x = x + 1;
5     a = y * y;
6     z = 8 * x + 24;
7     printf("%d %d\n", a, z);
8 }
```

c. Which line of code is **loop-invariant**? (Give the line number)

Line 5.

d. Which variable is the **base induction variable**?

x is the base induction variable.

e. Which variable is a **derived induction variable**?

z is a derived induction variable, with triple <x, 8, 24>.

f. Rewrite the program after **loop invariant code motion** and **induction variable optimizations** mentioned in class.

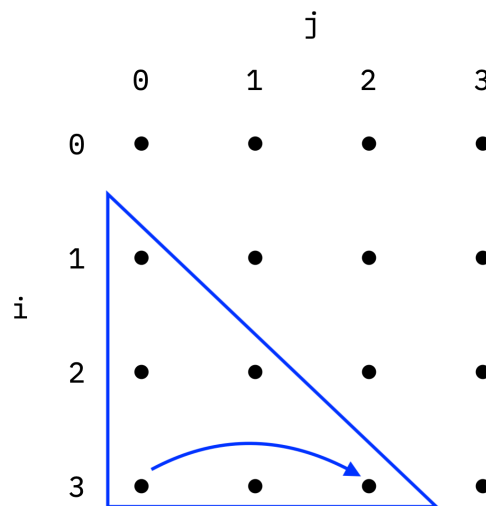
```
1 z = 24;
2 y = 5;
3 a = y * y;
4 while (z < 104) {
5     z = z + 8;
6     printf("%d %d\n", a, z);
7 }
```

## 2. Parallelization

Consider the following loops, where  $A[i, j]$  refers to the element in the  $i$ -th row and  $j$ -th column in a two-dimensional array.

```
for (i = 0; i < n; i += 1) {  
    for (j = 0; j < i; j += 1) {  
        A[i, j] = A[i, j - 2] + 3;  
    }  
}
```

- a. Assume  $n = 4$ . In the grid below, circle the **iteration space** for the loops and draw the **distance vectors**. You may ignore out-of-range cases.



- b. What is the **distance vector** for these loops?

$dv = [0, 2]$

- c. Which of the loops (inner and/or outer) can be parallelized into a for-all loop?

Only the outer loop (the  $i$  loop) can be parallelized into a for-all loop.